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Applicant: Seigo ARITA
Title: SECURE PARAMETER
GENERATING DEVICE AND
PARAMETER GENERATING
METHOD IN ALGEBRAIC CURVE
CRYPTOGRAPHY

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Seigo ARITA

Enclosed are:

- [X] Specification, Claim(s), and Abstract (100 pages).
- [X] Formal drawings (6 sheets, Figures 1-6).
- [X] Declaration and Power of Attorney (2 pages).
- [X] Assignment of the invention to NEC CORPORATION.
- [X] Assignment Recordation Cover Sheet.
- [X] Claim for Convention Priority w/ 1 certified document.
- [X] Information Disclosure Statement.
- [X] Form PTO-1449 with copies of 3 listed reference(s).

The filing fee is calculated below:

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Basic Fee				\$690.00	\$690.00
Total Claims:	39	- 20	= 19	x \$18.00	= \$342.00
Independents:	7	- 3	= 4	x \$78.00	= \$312.00
If any Multiple Dependent Claim(s) present:				+ \$260.00	= \$0.00
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SECURE PARAMETER GENERATING DEVICE AND PARAMETER
GENERATING METHOD IN ALGEBRAIC CURVE CRYPTOGRAPHY

BACKGROUNDS OF THE INVENTION

5 FIELD OF THE INVENTION

 The present invention relates to a secure
parameter generating device, a generating method, and a
storing medium in a discrete logarithm cryptography
(hereinafter, referred to an algebraic curve
10 cryptography), and more particularly to a secure
parameter generating device and its generating method in
a discrete logarithm cryptography using Jacobian group
of algebraic curve.

DESCRIPTION OF THE RELATED ART

15 A discrete logarithm cryptography is a public
key system based on the difficulty of a discrete
logarithm problem on a given finite field. In order to
keep the security of cryptography, the order of the
finite field must be almost a prime number, that is, a
20 factor of small integer and large integer. The algebraic
curve cryptography that is one of the discrete logarithm
cryptography needs to use an algebraic curve such that
the order of the Jacobian group is almost a prime number.

 In the case of an elliptic curve that is the
25 simplest algebraic curve, an efficient algorithm of
calculating the order of the Jacobian group over any
elliptic curve is known. The detailed description is

shown in, for example, "Counting points on elliptic curves over finite fields", Journal de Theorie des Nombres, de Bordeaux 7 (1995), 219-254, Institut de Mathematique de Bordeaux, written by Rene Schoof. The
5 elliptic curve such that the order of the Jacobian group is almost a prime factor can be obtained as follows, by using the above algorithm.

1. Generate a random elliptic curve E.
2. Calculate the order n of the Jacobian group

10 of E.

3. If n is almost a prime number, output E; otherwise, return to 1.

15 In the case of an algebraic curve other than an elliptic curve, no efficient algorithm of calculating the order of the Jacobian group is known except for one hyper-elliptic curve. Therefore, the algebraic curve which can be used in the algebraic curve cryptography is limited to an elliptic curve or one exceptional hyper
20 elliptic curve.

As for the h-fold operation of the elements in the Jacobian group, "Software Installation of Discrete Logarithm Cryptography Using C_{ab} curve" written by Arita, Yoshikawa, and Miyauchi, pp.573-578, Security Symposium
25 on Cryptography and Information in 1999, is known.

Further, the technique disclosed in Japanese Patent Publication Laid-Open (Kokai) No. Heisei 6-282226

comprises a step of selecting any prime number, storing
an encryption key corresponding to the prime number into
the public file device, generating a decoding key list
corresponding to the prime number and the encryption key,
5 and storing the decoding key list together with the
prime number into a decoder, wherein an encoder obtains
a public key of a receiver (decoder) from the public
file, to multiply the plaintext on an elliptic curve,
its value is sent to the decoder as a cryptogram, and
10 the decoder computes a parameter of the elliptic curve
from the cryptogram and selects a decoding key
corresponding to the parameter by use of the decoding
key list, thereby obtaining the plaintext from the value
obtained by multiplying the cryptogram by the elliptic
15 curve, using Chinese residue theorem.

The above mentioned conventional technique
limits the usable algebraic curves to an elliptic curve
or one of exceptional hyper-elliptic curve. Since the
elliptic curve and the hyper-elliptic curve are
20 extremely particular algebraic curve from the viewpoint
of the whole algebraic curves and this narrows the
target for cryptanalysis, there arises a security
problem of an algebraic curve cryptography.

SUMMARY OF THE INVENTION

An object of the present invention is to make it
possible to use a higher and complicated algebraic curve

which couldn't be used, for an algebraic curve cryptography, and to provide a secure parameter generating device in an algebraic curve cryptography for improving the security of the algebraic curve cryptography.

Further, another object of the present invention is to make it possible to use a higher and complicated algebraic curve which couldn't be used, for an algebraic curve cryptography, and to provide a secure parameter generating method in the algebraic cryptography for improving the security of the algebraic curve cryptography.

According to the first aspect of the invention, a secure parameter generating device in an algebraic curve cryptography, comprises

an input means for receiving two different prime numbers (a, b) specifying degree of complexity of a curve and size (n) of an encryption key to be used,

a Stickelberger element computing device for computing a Stickelberger element (ω) in an ab cyclotomic, based on the prime number (a) and the prime number (b),

a Jacobian addition candidate value computing device for computing Jacobian addition candidate value j corresponding to the two different prime numbers a and b, and a prime number p corresponding to the Jacobian addition candidate value j, based on the prime number

(a), the prime number (b), the size (n) of an encryption key, and the Stickelberger element (ω),

an order candidate value computing device for computing a class H consisting of a plurality of candidate values for order of a Jacobian group of an algebraic curve specified by the prime number a and the prime number b, based on the prime number a, the prime number b, and the Jacobian addition candidate value j,

a security judging device for searching for a candidate value h meeting a security condition such as almost prime number characteristic from the class H, according to the class H,

a parameter deciding device for computing a parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h, of the algebraic curves specified by the prime number a, the prime number b, and the prime number p, based on the prime number a, the prime number b, the prime number p, and the candidate value h, and

an output device for supplying the parameter of the algebraic curve computed by said parameter deciding device.

In the preferred construction, a secure parameter generating device in an algebraic curve cryptography further comprises

an a-storing means, a b-storing means, and an n-storing means for respectively storing the prime number

a, the prime number b, and the size n of the encryption key received by said input means,

a ω -storing means for storing a Stickelberger element ω computed by said Stickelberger element
5 computing device,

a p-storing means and a j-storing means for respectively storing the prime number p and the Jacobian addition candidate value j computed by said Jacobian addition candidate value computing device,

10 an H-storing means for storing the class H computed by said order candidate value computing device, and

an h-storing means for storing the candidate value h found by said security judging device.

15 In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

said Stickelberger element computing device for computing the Stickelberger element ω by use of the
20 equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
25 indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b.

In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

5 said Jacobian addition candidate value computing device for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the
10 prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$.

15 In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

20 said Stickelberger element computing device for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{\{-t^{-1}\}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
25 (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b , and

 said Jacobian addition candidate value computing

device for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$.

In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

said order candidate value computing device for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

said Stickelberger element computing device for computing the Stickelberger element ω by use of the

equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{\{-t^{-1}\}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b , and

10 said order candidate value computing device for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{\{K|Q\}}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

20 In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

25 said Jacobian addition candidate value computing device for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the

prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$, and

5 said order candidate value computing device for
computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-$
10 $\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1
to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

15 In another preferred construction, secure
parameter generating device in an algebraic curve
cryptography comprises

 said Stickelberger element computing device for
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20 equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{\{-t^{-1}\}}$ (where, t runs
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used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
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25 indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
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said order candidate value computing device for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

said parameter deciding device for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number

p, and the candidate value h, generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} y^a + \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h-fold of an element in the Jacobian group indicated by the point G, and supplying p, ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h, of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

said Stickelberger element computing device for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b, and

said parameter deciding device for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on

the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} y^a + \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises said Jacobian addition candidate value computing device for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$, and

said parameter deciding device for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1

with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y_a + \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

said order candidate value computing device for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$, and

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primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a, the prime number b, the prime number p, and the candidate value h, generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a + \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h-fold of an element in the Jacobian group indicated by the point G, and supplying p, ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h, of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

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said Stickelberger element computing device for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b,

said Jacobian addition candidate value computing device for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$, and

said parameter deciding device for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^l y^a + \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^l , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating device in an algebraic curve

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said order candidate value computing device for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{\{K|Q\}}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$, and

said parameter deciding device for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$

+ $\zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^l , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

said Jacobian addition candidate value computing device for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$,

said order candidate value computing device for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab

cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H=\{h_1, h_2, \dots, h_{2ab}\}$, and

said parameter deciding device for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a + \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating device in an algebraic curve cryptography comprises

said Stickelberger element computing device for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{\{-t^{-1}\}}$ (where, t runs on a typical series of irreducible residue class with ab

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15

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20 Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$, and
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said parameter deciding device for requiring the

primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a, the prime number b, the prime number p, and the candidate value h, generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a + \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h-fold of an element in the Jacobian group indicated by the point G, and supplying p, ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h, of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

According to the second aspect of the invention, a secure parameter generating method in an algebraic curve, comprises the steps of

a Stickelberger element computing procedure for computing a Stickelberger element ω in an ab cyclotomic, respectively based on two different prime numbers a and b specifying degree of complexity of curve,

a Jacobian addition candidate value computing procedure for computing Jacobian addition candidate value j corresponding to the two different prime numbers a and b, and a prime number p corresponding to the Jacobian addition candidate value j, respectively based on the prime number a, the prime number b, the size n of

an encryption key, and the Stickelberger element ω ,

an order candidate value computing procedure for
computing a class H consisting of a plurality of
candidate values for order of a Jacobian group of an
algebraic curve specified by the prime number a and the
prime number b, respectively based on the prime number a,
the prime number b, and the Jacobian addition candidate
value j,

a security judging procedure for searching for a
candidate value h meeting a security condition such as
almost prime number characteristic from the class H,
according to the class H, and

a parameter deciding procedure for computing a
parameter of an algebraic curve whose order of the
Jacobian group is in accord with the candidate value h,
of the algebraic curves specified by the prime number a,
the prime number b, and the prime number p, respectively
based on the prime number a, the prime number b, the
prime number p, and the candidate value h.

In the preferred construction, a secure
parameter generating method in an algebraic curve
cryptography comprises

a procedure for storing a Stickelberger element
 ω computed by said Stickelberger element computing
procedure into said ω -storing means,

a procedure for respectively storing the prime
number p and the Jacobian addition candidate value j

computed by said Jacobian addition candidate value
computing procedure into said p-storing means and j-
storing means,

5 a procedure for storing the class H computed by
said order candidate value computing procedure into said
H-storing means, and

a procedure for storing the candidate value h
found by said security judging procedure into said h-
storing means.

10 In another preferred construction, a secure
parameter generating method in an algebraic curve
cryptography comprises

15 said Stickelberger element computing procedure
for computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{\{-t^{-1}\}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
20 indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
(ζ is the primitive ab root of 1)), based on the prime
number a and the prime number b.

25 In another preferred construction, a secure
parameter generating method in an algebraic curve
cryptography comprises

said Jacobian addition candidate value computing
procedure for generating α at random, which is an

algebraic integer γ generating a prime ideal of a
cyclotomic K generated by the primitive ab root of 1 and
whose absolute norm becomes the prime number p of bit
length $2n/(a-1)(b-1)$ or so, based on the prime number a ,
5 the prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$.

In another preferred construction, a secure
10 parameter generating method in an algebraic curve
cryptography comprises

said Stickelberger element computing procedure
for computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{\{-t^{-1}\}}$ (where, t runs
15 on a typical series of irreducible residue class with ab
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exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
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20 (ζ is the primitive ab root of 1)), based on the prime
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25 cyclotomic K generated by the primitive ab root of 1 and
whose absolute norm becomes the prime number p of bit
length $2n/(a-1)(b-1)$ or so, based on the prime number a ,

the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$.

5 In another preferred construction, a secure parameter generating method in an algebraic curve cryptography comprises

10 said order candidate value computing procedure for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

15 In another preferred construction, a secure parameter generating method in an algebraic curve cryptography comprises

20 said Stickelberger element computing procedure for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{\{-t^{-1}\}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t

25

indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b , and

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for computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
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cyclotomic K), as for each k that is an integer from 1
10 to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
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length $2n/(a-1)(b-1)$ or so, based on the prime number a ,
the prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
25 Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$, and

 said order candidate value computing procedure

for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

In another preferred construction, a secure parameter generating method in an algebraic curve cryptography comprises

said Stickelberger element computing procedure for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{\{-t^{-1}\}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b ,

said Jacobian addition candidate value computing procedure for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit

length $2n/(a-1)(b-1)$ or so, based on the prime number a ,
the prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
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Jacobian group of an algebraic curve specified by the
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cyclotomic K), as for each k that is an integer from 1
to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

In another preferred construction, a secure
parameter generating method in an algebraic curve
cryptography comprises

said parameter deciding procedure for requiring
the primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a , the prime number b , the prime number
 p , and the candidate value h , generating a random point
 G over an algebraic curve defined by the equation $\zeta_a^{-1} y^a$
 $+ \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h -fold of an element in the Jacobian group

indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating method in an algebraic curve cryptography comprises

said Stickelberger element computing procedure for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{\{-t^{-1}\}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b , and

said parameter deciding procedure for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} y^a + \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively,

computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating method in an algebraic curve cryptography comprises

said Jacobian addition candidate value computing procedure for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$, and

said parameter deciding procedure for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} y^a + \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a

inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating method in an algebraic curve cryptography comprises

said order candidate value computing procedure for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$, and

said parameter deciding procedure for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$

+ $\zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^l , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

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length $2n/(a-1)(b-1)$ or so, based on the prime number a ,
the prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$, and

said parameter deciding procedure for requiring
the primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a , the prime number b , the prime number
 p , and the candidate value h , generating a random point
 G over an algebraic curve defined by the equation $\zeta_a^{-1} y^a$
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the Jacobian group is in accord with the candidate value
 h , of the algebraic curves specified by the prime number
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used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b ,

said order candidate value computing procedure for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$, and

said parameter deciding procedure for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a + \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of

the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

5 In another preferred construction, a secure parameter generating method in an algebraic curve cryptography comprises

 said Jacobian addition candidate value computing procedure for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$,

 said order candidate value computing procedure for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{\{K|Q\}}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$, and

said parameter deciding procedure for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a, the prime number b, the prime number p, and the candidate value h, generating a random point G over an algebraic curve defined by the equation $\zeta_a^1 Y^a + \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h-fold of an element in the Jacobian group indicated by the point G, and supplying p, ζ_a^1 , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h, of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

In another preferred construction, a secure parameter generating method in an algebraic curve cryptography comprises

said Stickelberger element computing procedure for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime

number a and the prime number b ,

said Jacobian addition candidate value computing procedure for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$,

said order candidate value computing procedure for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$, and

said parameter deciding procedure for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$

+ $\zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^l , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

10 According to another aspect of the invention, a computer readable memory storing a program for generating a secure parameter in an algebraic curve cryptography, to run the program on a computer, the program comprises the steps of

15 a Stickelberger element computing procedure for computing a Stickelberger element ω in an ab cyclotomic, respectively based on two different prime numbers a and b specifying degree of complexity of curve,

20 a Jacobian addition candidate value computing procedure for computing Jacobian addition candidate value j corresponding to the two different prime numbers a and b , and a prime number p corresponding to the Jacobian addition candidate value j , respectively based on the prime number a , the prime number b , the size n of an encryption key, and the Stickelberger element ω ,

25 an order candidate value computing procedure for computing a class H consisting of a plurality of

candidate values for order of a Jacobian group of an algebraic curve specified by the prime number a and the prime number b , respectively based on the prime number a , the prime number b , and the Jacobian addition candidate value j ,

a security judging procedure for searching for a candidate value h meeting a security condition such as almost prime number characteristic from the class H , according to the class H , and

a parameter deciding procedure for computing a parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a , the prime number b , and the prime number p , respectively based on the prime number a , the prime number b , the prime number p , and the candidate value h .

Other objects, features and advantages of the present invention will become clear from the detailed description given herebelow.

BRIEF DESCRIPTION OF THE DRAWINGS

The present invention will be understood more fully from the detailed description given herebelow and from the accompanying drawings of the preferred embodiment of the invention, which, however, should not be taken to be limitative to the invention, but are for explanation and understanding only.

In the drawings:

Fig. 1 is a block diagram showing the form of the first embodiment according to the present invention;

5 Fig. 2 is a flow chart showing the operation of a Stickelberger element computing device;

Fig. 3 is a flow chart showing an operation of the Jacobian additive candidate value computing device;

Fig. 4 is a flow chart showing the operation of the order candidate value computing device;

10 Fig. 5 is a flow chart showing the parameter deciding device;

Fig. 6 is a block diagram showing the form of the third embodiment of the present invention.

15 DESCRIPTION OF THE PREFERRED EMBODIMENT

The preferred embodiment of the present invention will be discussed hereinafter in detail with reference to the accompanying drawings. In the following description, numerous specific details are set forth in order to provide a thorough understanding of the present invention. It will be obvious, however, to those skilled in the art that the present invention may be practiced without these specific details. In other instance, well-known structures are not shown in detail in order to unnecessary obscure the present invention.

25

First, the principle of the present invention will be described.

The present invention is to efficiently search for an algebraic curve such that the order of the Jacobian group is almost a prime number, from the class of an algebraic curve having the definition expression such as $\alpha Y^a + \beta X^b + 1 = 0$, and to make it possible to use a higher and complicated algebraic curve that couldn't be used, for an algebraic curve cryptography. Here, the parameters a and b indicate the degree of complexity of curves.

The algebraic curve over a finite field F_q of the order q , which has the definition expression such as $\alpha Y^a + \beta X^b + 1 = 0$, is defined as $C(q, \alpha, \beta)$. As for the algebraic curve $C(q, \alpha, \beta)$, the order of the Jacobian group can be designed using the description about its L function by use of the Jacobian addition.

Hereafter, for brief description, assume that $q := p$ (p is expressed by q) is a prime number, and that the expression, $p \equiv 1 \pmod{\text{LCM}(a, b)}$ is satisfied (LCM is the least common multiple). Further, the primitive ab root of 1 is defined as ζ . The prime number p is completely factorized into m pieces of prime ideals, P_1, P_2, \dots, P_m in a cyclotomic $\mathbb{Q}(\zeta)$. Here, the number m is the number of irreducible residue classes of the divisor ab .

The generator w of the multiplication group F_p^* of the finite field F_p is fixed, and the index χ_s of F_p^* , as for the rational number such that $(p-1)s$ becomes an

integer, is defined as $\chi_s(w) = \exp(2\pi i s)$ (where i is an imaginary number). Assuming that $\chi_s(0) = 0$ (s : when it is not an integer), $=1$ (s : when it is an integer), the domain is expanded on the whole F_p . As for the integer $l=1, 2, \dots, a-1$ and the integer $m=1, 2, \dots, b-1$, the expression, $j_p(l, m) = \sum_{\{l+v_1+v_2=0\}} \chi_{l/a}(v_1) \chi_{m/b}(v_2)$ is called as Jacobian addition. Where, v_1 and v_2 run on $v_1, v_2 \in F_p$ meeting the equation $l+v_1+v_2=0$. At this time, it is well known that the L function $L_p(U)$ of $C(p, \alpha, \beta)$ can be expressed by using the Jacobian addition as follows.

$$L_p(U) = \prod_{l=1, 2, \dots, a-1, m=1, 2, \dots, b-1} (1 + \chi_{l/a}(\alpha^{-1}) \chi_{m/b}(\beta^{-1}) j_p(l, m) U).$$
 Therefore, the order h of the Jacobian group of $C(p, \alpha, \beta)$ is given by $h = L_p(1) = \prod_{l=1, 2, \dots, a-1, m=1, 2, \dots, b-1} (1 + \chi_{l/a}(\alpha^{-1}) \chi_{m/b}(\beta^{-1}) j_p(l, m))$. It is necessary to calculate the Jacobian addition $j_p(l, m)$, in order to require the order of the Jacobian group. However, since it is impossible to directly calculate the Jacobian addition $j_p(l, m)$ according to the definition expression, from the viewpoint of the volume of calculation, the Stickelberger element as for the following Jacobian addition is used.

Assume that $[\lambda]$ indicates the maximum integer not exceeding the rational number λ and that $\langle \lambda \rangle$ indicates the fraction part $\lambda - [\lambda]$ of the rational number λ . Further, assume that σ_t indicates the Galois mapping

$\zeta \rightarrow \zeta^t$ of the cyclotomic field $Q(\zeta)$. The Stickelberger element $\omega(a, b)$ that is the generator of the group ring $Z[\text{Gal}(Q(\zeta)|Q)]$ is defined as $\omega(a, b) = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t}^{-1}$. Where, t runs on the typical series of the irreducible residue class with the divisor ab .

It is well known that the expression $(j_p(l, m)) = P^{\omega(a, b)}$ is satisfied as the ideal of the cyclotomic field $Q(\zeta)$. Where, P is the prime ideal on p . By the above expression, $j_p(l, m)$ is necessarily resolved except for the $2ab$ root of 1. Of the results, the degree of freedom for ab root can be obtained by the degree of freedom of the coefficient $\alpha, \beta \in F_q$ of $C(p, \alpha, \beta)$.

In these ways, the search algorithm of the following secure curve $C(p, \alpha, \beta)$ can be obtained.

The search algorithm of the secure curve $C(p, \alpha, \beta)$

input: the number of Jacobian bits n

output: p, α, β

(1) $g \leftarrow (a-1)(b-1)/2$

(2) The candidate j of the Jacobian addition as for the prime number p of some n/g bit or the like is searched for by using the calculation algorithm of the candidate value of the Jacobian addition as described later:

$(p, j) \leftarrow \{\text{calculation algorithm of the candidate value of the Jacobian addition}\}(n/g)$.

(3) as for the respective $k = 0, 1, \dots, ab$,

$h_k \leftarrow \prod_{l=1, 2, \dots, a-1, m=1, 2, \dots, b-1} (1 + (-\zeta)^k j)$

(4) Check whether there is an almost prime number h_k in

$\{ h_0, h_1, \dots, h_{ab} \}$. If there is none, return to (1). If there is, $h := h_k$ is defined.

(5) The symbols ζ_a, ζ_b are respectively defined as a-root of 1 and b-root of 1 in F_p . Check whether the order of the Jacobian group of the curve $C(p, \zeta_a^{-1}, \zeta_b^m): \zeta_a^{-1} y^a + \zeta_b^m x^b + 1 = 0$ is equal to h , as for the respective $l = 0, 1, \dots, a-1$ and the respective $m = 0, 1, \dots, b-1$. If it is equal, output $p, \alpha = \zeta_a^{-1}, \beta = \zeta_b^m$ and finish the operation. If such l and m don't exist, return to (2).

In the calculation algorithm of the candidate value of the Jacobian addition used in the above, the candidate value of the Jacobian addition is required by using the above-mentioned Stickelberger element $\omega(a, b) = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t}^{-1}$.

The calculation algorithm of the candidate value of the Jacobian addition is as follows.

input: the number of bits m ,

output: p, j ,

(1) $\omega \leftarrow \sum_t (\langle t/a \rangle + \langle t/b \rangle) \sigma_{-t}^{-1}$,

(2) Generate $\gamma_0 = \sum_{i=0}^{m-1} c_i \zeta^i$ ($-10 < c_i < 10$) at random.

(3) as for the respective $i = 1, 2, \dots$,

$\gamma \leftarrow \gamma_0 + I$,

$p \leftarrow \text{Norm}_{\mathbb{Q}(\zeta)|\mathbb{Q}}(\gamma)$,

Is p smaller than m bit or so?

yes \rightarrow continue,

Is p larger than m bit or so?

yes \rightarrow to (2),

Is p a prime number?

no \rightarrow continue,

(4) Output $j \leftarrow \gamma^\omega$, p and j , and finish.

This time, the form of the first embodiment of
5 the present invention will be described with reference
to the accompanying drawings. Fig. 1 is a block diagram
showing the form of the first embodiment.

With reference to Fig. 1, the form of the first
embodiment of the present invention comprises a
10 Stickelberger element computing device 11, a Jacobian
addition candidate value computing device 12, an order
candidate value computing device 13, a security judging
device 14, a parameter deciding device 15, a memory 16,
an input device 17, an output device 18, and a central
15 processing unit 19.

The memory 16 includes a a-storing file 161, a
b-storing file 162, a ω -storing file 163, a j-storing
file 164, an H-storing file 165, an h-storing file 166,
a p-storing file 167, and an n-storing file 168.

20 Hereinafter, assume that a known method is used
for the norm arithmetic $N_{Q(\zeta)|Q}$ and four fundamental
arithmetic rules of algebraic number in the cyclotomic
field $Q(\zeta)$, arithmetic of the function of the Galois
group $G(Q(\zeta)|Q)$ for the cyclotomic field $Q(\zeta)$, and
25 addition and multiplication in the group ring $Z[G(Q(\zeta)|Q)]$
on the Galois group $G(Q(\zeta)|Q)$ of the integer ring Z
coefficient.

The operation of the form of a first embodiment according to the present invention will be described this time.

Fig. 2 is a flow chart showing the operation of the Stickelberger element computing device 11. Fig. 3 is a flow chart showing the operation of the Jacobian addition candidate value computing device 12. Fig. 4 is a flow chart showing the operation of the order candidate value computing device 13. Fig. 5 is a flow chart showing the operation of the parameter deciding device 15.

The description will be made in the case where two different prime numbers, $a=3$, $b=7$, specifying the degree of complexity of a curve, and the size $n=160$ of an encryption key to be used are supplied from the input device 17. The supplied a and b are temporarily stored in the a -storing file 161 and the b -storing file 162 respectively, through the central processing unit 19. Further, a variable found in the following description is stored in the memory 16.

The Stickelberger element computing device 11 obtains $a=3$, $b=7$ from the a -storing file 161 and the b -storing file 162, according to the operation as shown in Fig. 2, and operates as follows.

A typical series $\{1, 2, 4, 5, 8, 10, 11, 13, 16, 17, 19, 20\}$ of the irreducible residue class with $a \cdot b = 3 \times 7 = 21$ used for the variable L as the divisor is stored

in Step S21 of Fig. 2.

As for the respective integers t included in the variable $L=\{1, 2, 4, 5, 8, 10, 11, 13, 16, 17, 19, 20\}$ in Step 22 of Fig. 2, for example, as for $t=1$, since
5 $[<1/3>+<1/7>] = [1/3+1/7]=[10/21]=0$, 0 is stored in the variable m ; since $-1^{-1} \equiv -1 \equiv 20 \pmod{21}$, 20 is stored in the variable s ; since $0 \times \sigma_{20} = 0$, 0 is stored in the variable λ_1 .

As for the other t , since

10 $[<2/3>+<2/7>]=[2/3+2/7]=[20/21]=0$, 0 is stored in the variable λ_2 ; since $[<4/3>+<4/7>]=[1/3+4/7]=[19/21]=0$, 0 is stored in the variable λ_4 ; since
 $[<5/3>+<5/7>]=[2/3+5/7]=[29/21]=1$ and $(-5)^{-1} \equiv 16^{-1} \equiv 4 \pmod{21}$, σ_4 is stored in the variable λ_5 ; since
15 $[<8/3>+<8/7>]=[2/3+1/7]=[17/21]=0$, 0 is stored in the variable λ_8 ; since $[<10/3>+<10/7>]=[1/3+3/7]=[16/21]=0$, 0 is stored in the variable λ_{10} ; since
 $[<11/3>+<11/7>]=[2/3+4/7]=[26/21]=1$ and $(-11)^{-1} \equiv 10^{-1} \equiv 19 \pmod{21}$, σ_{19} is stored in the variable λ_{11} ; since
20 $[<13/3>+<13/7>]=[1/3+6/7]=[25/21]=1$ and $(-13)^{-1} \equiv 8^{-1} \equiv 8 \pmod{21}$, σ_8 is stored in the variable λ_{13} ; since
 $[<16/3>+<16/7>]=[1/3+2/7]=[13/21]=0$, 0 is stored in the variable λ_{16} ; since $[<17/3>+<17/7>]=[2/3+3/7]=[23/21]=1$ and $(-17)^{-1} \equiv 4^{-1} \equiv 16 \pmod{21}$, σ_{16} is stored in the
25 variable λ_{17} ; since $[<19/3>+<19/7>]=[1/3+5/7]=[22/21]=1$ and $(-19)^{-1} \equiv 2^{-1} \equiv 11 \pmod{21}$, σ_{11} is stored in the variable λ_{19} ; and since

$[<20/3>+<20/7>]=[2/3+6/7]=[32/21]=1$ and $(-20)^{-1} \equiv 1^{-1} \equiv 1 \pmod{21}$, σ_1 is stored in the variable λ_{20} , in the same way.

5 The total $\omega = \sigma_4 + \sigma_{19} + \sigma_8 + \sigma_{16} + \sigma_{11} + \sigma_1$ of
the whole data stored in the respective variables $\lambda_1, \lambda_2,$
 $\lambda_4, \lambda_5, \lambda_8, \lambda_{10}, \lambda_{11}, \lambda_{13}, \lambda_{16}, \lambda_{17}, \lambda_{19}, \lambda_{20}$ is computed
in Step S23 of Fig. 2. Here, the total means the total
in the group ring $\mathbb{Z} [G(\mathbb{Q}(\zeta) | \mathbb{Q})]$, indicating the total
of the coefficients of the respective σ_i with the
10 respective σ_i regarded as symbols. The arithmetic result
 ω is temporarily stored in the ω -storing file 163
through the central processing unit 19.

The Jacobian addition candidate value computing
device 12 obtains $a=3, b=7, n=160, \omega=\sigma_4 + \sigma_{19} + \sigma_8 + \sigma_{16}$
15 $+ \sigma_{11} + \sigma_1$ from the a-storing file 161, the b-storing
file 162, the n-storing file 168, and the ω -storing file
163 and computes the candidate value j of the Jacobian
addition, according to the processing as shown in Fig. 3,
as follows.

20 Since $ab=21$, the primitive 21^{st} power root of 1
is stored in the variable ζ , and since $2n / (a-1)(b-1) =$
 $26.6\dots$, 27 is stored in the variable m , in Step 31 of
Fig. 3.

The random integer of the cyclotomic field $\mathbb{Q}(\zeta)$
25 is stored in the variable γ_0 as follow, in Step S32 of
Fig. 3. The variable γ_0 is initialized to 0; the random
number $r_0 = -2$ is generated as for $t=0, r_0 \zeta^0 = -2$ is

added to γ_0 , so to require $\gamma_0 = -2$; the random number $r_1 = 2$ is generated as for $t=1$, $r_1 \zeta^1 = 2 \zeta$ is added to γ_0 , so to require $\gamma_0 = -2 + 2\zeta$; and the same operation is repeated until $t=11$, so to require $\gamma_0 = -2 + 2\zeta - \zeta^2 + 2\zeta^3 + 2\zeta^5 - \zeta^6 - \zeta^7 - 2\zeta^8 + 2\zeta^9 - \zeta^{11}$, in Step S32 of Fig. 3.

The following operation will be performed on the respective integers $i=0, 1, 2, \dots$, in Step S33 of Fig. 3. As for $i=0$, $\gamma_0 + 0$ is stored in the variable γ , so to obtain $\gamma = -2 + 2\zeta - \zeta^2 + 2\zeta^3 + 2\zeta^5 - \zeta^6 - \zeta^7 - 2\zeta^8 + 2\zeta^9 - \zeta^{11}$, to compute the norm $N_{Q(\zeta)|Q}(\gamma)$. The resultant 129571513 is stored in the p-storing file 167, the number of bits 29 of $p = 129571513$ is stored in the variable 1. That $l=29$ and $m=27$ or so is confirmed. When $p = 129571513$ is factorized into prime factors in the known way, $p = 129571513 = 43 \times 211 \times 14281$ is obtained. Since $p = 129571513$ is not a prime number, the operation as for $i = 0$ is finished, and as for $i = 1$, the same operation will be repeated. In the form of this embodiment, the same operation is continued until $i = 2$. As for $i = 2$, $\gamma_0 + 2$ is stored in the variable γ , so to obtain $\gamma = 2\zeta - \zeta^2 + 2\zeta^3 + 2\zeta^5 - \zeta^6 - \zeta^7 - 2\zeta^8 + 2\zeta^9 - \zeta^{11}$, to compute the norm $N_{Q(\zeta)|Q}(\gamma)$. The resultant 163255597 is stored in the p-storing file 167, and the number of bits 28 of $p = 163255597$ is stored in the variable 1. Since $l=28$ and $m=27$ or so, and $p = 163255597$ is determined as a prime number (a known method is used

for judgment of a prime number), the operation of Step S33 will be finished.

In Step S34 of Fig. 3, the Stickelberger element $\omega = \sigma_4 + \sigma_{19} + \sigma_8 + \sigma_{16} + \sigma_{11} + \sigma_1$ is adopted to work on the value $2\zeta - \zeta^2 + 2\zeta^3 + 2\zeta^5 - \zeta^6 - \zeta^7 - 2\zeta^8 + 2\zeta^9 - \zeta^{11}$ of the variable γ and the result is stored in the j-storing file 164.

Namely, since $j = \sigma_4(\gamma) \sigma_{19}(\gamma) \sigma_8(\gamma) \sigma_{16}(\gamma) \sigma_{11}(\gamma) \sigma_1(\gamma) = -11346 + 4158\zeta + 9337\zeta^2 - 10930\zeta^3 + 3060\zeta^4 + 11132\zeta^5 - 1408\zeta^6 - 10000\zeta^7 + 7506\zeta^8 + 1237\zeta^9 - 9894\zeta^{10} + 16406\zeta^{11}$, the content of the j-storing file 164 becomes $-11346 + 4158\zeta + 9337\zeta^2 - 10930\zeta^3 + 3060\zeta^4 + 11132\zeta^5 - 1408\zeta^6 - 10000\zeta^7 + 7506\zeta^8 + 1237\zeta^9 - 9894\zeta^{10} + 16406\zeta^{11}$.

The order candidate value computing device 13 obtains a, b, j respectively from the a-storing file 161, the b-storing file 162, and the j-storing file 164, according to the processing as shown in Fig. 4, and computes each candidate value for the order of the Jacobian group, as follows.

Since $ab=21$, the primitive 21st power root of 1 is stored in the variable ζ , in Step S41 of Fig. 4.

In Step S42 of Fig. 4, $N_{Q(\zeta)|Q} (1 + (-\zeta)^k j)$ is computed as for the respective integers $k=1, \dots, 2ab=42$, by using the Jacobian addition candidate value j, and the result is stored in the variable h_k . Namely, since $N_{Q(\zeta)|Q} (1 + (-\zeta) j)$

=18945750554224674862720917379214050968749547249577 as
for $k=1$,

18945750554224674862720917379214050968749547249577 is
stored in the variable h_1 , and since $N_{Q(\zeta)}|_Q (1 + (-\zeta)^2 j)$
5 = 18928969305265796978830941938772180777050417721949 as
for $k=2$,

18928969305265796978830941938772180777050417721949 is
stored in the variable h_2 .

10 Hereinafter, in the same way,

18939442397757559639176586128404383479076142135761 is
stored in the variable h_3 ;

18935060345406437247984249590121980321244862496761 is
stored in the variable h_4 ;

15 18935622676852726684902816970612470237474541809664 is
stored in the variable h_5 ;

18931936903665705475581647305574444786263237069081 is
stored in the variable h_6 ;

20 18929560654771860101383318185997674116929626012889 is
stored in the variable h_7 ;

18939150203650250186166315242126355786799280592469 is
stored in the variable h_8 ;

18932675807273674693936115572103379669380378369473 is
stored in the variable h_9 ;

25 18942309965821405414970614992239749691042375170033 is
stored in the variable h_{10} ;

18934229290635176830764035532046510839791719442389 is

18929984863788418751836156261712299372083231633577 is
stored in the variable h_{25} ;

18929422531793648170111228339741198150094983499776 is
stored in the variable h_{26} ;

```
5      18933107954541528865152848804062672753166448460761 is
      stored in the variable  $h_{27}$ ;
```

18935483634705487053043563594391048299333735703993 is
stored in the variable h_{28} ;

```

18925896848340062851972136696783348221127455098349 is
10 stored in the variable h29;

```

18932368490475205159124453933007681555744686326777 is
stored in the variable h_{30} ;

18922739336864448742750281538719599103232717642873 is
stored in the variable h_{31} ;

```
15      18930815175217344826609492375186423724694014551957 is
      stored in the variable  $h_{32i}$ ;
```

```
18929210510360406226057659372472230885175421077009 is
stored in the variable h33;
```

```

18926967327936730178250537884862137815188718140673 is
20 stored in the variable  $h_{34}$ ;

```

18934063763272126450623787600233843527396400812437 is
stored in the variable h_{35} ;

18939120559761876801054292506881700885415287701041 is
stored in the variable h_{36} ;

```
25      18928816315710623530089460607608797337081800632473 is
      stored in the variable h37;
```

18929656538570982720438072809652072203857571941789 is

stored in the variable h_{38} ;
18933352933862176606331230531189579186007983024249 is
stored in the variable h_{39} ;
18932310663274994445599743180032079937147687805121 is
5 stored in the variable h_{40} ;
18926381945702726406182624557022344113037957991709 is
stored in the variable h_{41} ; and
18931102681789095072229676262975577344314266433617 is
stored in the variable h_{42} , respectively.

10 Finally, the order candidate value computing
device 13 combines the contents of the variables h_1 to h_{42}
together as H and stores the same into the H-storing
file 165.

15 The security judging device 14 obtains the H
from the H-storing file 165, and searches for a
candidate value h meeting the security condition of
almost prime number characteristic from the order
candidate values h_1, h_2, \dots, h_{42} included in the H, and
20 stores the same into the h-storing file 166. In this
form of the embodiment, for brief description, the
security condition is considered as for the almost prime
number characteristic. By use of the known prime number
judging method, $h_{11} =$

25 18934229290635176830764035532046510839791719442389 is
judged to be a prime number, and the security judging
device 14 stores $h = h_{11} =$

18934229290635176830764035532046510839791719442389 into the h-storing file 166.

5 The parameter deciding device 15 obtains a, b, p, and h respectively from the a-storing file 161, the b-storing file 162, the p-storing file 167, and the h-storing file 166, and operates according to the processing as shown in Fig. 5.

10 In Step S51 of Fig. 5, 127994587 that is the primitive 3rd power root of 1 with p = 163255597 used as the divisor is stored in the variable ζ_3 , and 8342648 that is the primitive 7th power root of 1 with p = 163255597 used as the divisor is stored in the variable ζ_7 .

15 In Step S52 of Fig. 5, the following processing will be performed on the respective integers l=1, 2, 3 and the respective integers m=1, 2, 3, 4, 5, 6, 7.

20 When l=1 and m=1, $\zeta_3 = 127994587$ is stored in the variable ε , and $\zeta_7 = 8342648$ is stored in the variable η . The random element $\{151707017 + 104678491 x + 123646083 x^2 + 18753988 y + 87634493 x^3 + 61274336 x y + x^4, 138799785 + 145105684 x + 584395 x^2 + 80828873 y + 34715892 x^3 + 121885874 x y + 59787844 x^4 + x^2 y,$
25 $161162224 + 117150097 x + 100956100 x^2 + 89380061 y + 140032555 x^3 + 43367019 x y + y^2 \}$ of the Jacobian group of an algebraic curve defined by the expression $\varepsilon y^3 + \eta$

$x^7 + 1 = 127994587 y^3 + 8342648 x^7 + 1 = 0$ is generated,
and this is stored in the variable G, the power of
 $h=18934229290635176830764035532046510839791719442389$ in
the Jacobian group, on a point stored in the variable G
5 is computed, and the result $\{133659497 + 103424746 x +$
 $136032897 x^2 + 131029199 y + 24618867 x^3 + 114944034 x y$
 $+ x^4, 86125426 + 125891893 x + 19568269 x^2 + 27044314 y +$
 $80420960 x^3 + 137562092 x y + x^2 y, 53604112 + 65990501 x$
 $+ 51269221 x^2 + 55271502 y + 7974233 x^3 + 84922220 x y +$
10 $y^2\}$ is stored in the variable G.

Since the above content of the variable G is not
equal to the identity element $\{\}$ in the Jacobian group, ζ
 $\zeta_3 = 127994587$ is stored in the variable ε , and $\zeta_7^2 =$
 $8342648^2 \bmod 163255597 = 159772073$ is stored in the
15 variable η , as for $l = 1$ and $m = 2$, thereby repeating
the above processing.

In the case of the form of this embodiment, when
 $l = 2$ and $m = 2$, $\varepsilon = 35261009$ and $\eta = 159772073$ are
obtained, the power of

20 $h=18934229290635176830764035532046510839791719442389$ on
the point $G = \{4568071 + 141843715 x + 68256743 x^2 +$
 $71903501 y + 128953783 x^3 + 10781960 x y + x^4, 48272788 +$
 $45615229 x + 150692034 x^2 + 53973350 y + 11114765 x^3 +$
 $78550130 x y + 61331354 x^4 + x^2 y, 117552807 + 135448907$
25 $x + 64074711 x^2 + 141058974 y + 49208246 x^3 + 93940317 x$
 $y + y^2\}$ generated at random results in the identity
element $\{\}$, and the parameter deciding device 15

supplies $p=163255597$, $\varepsilon=35261009$, $\eta=159772073$ as the parameters of a secure algebraic curve.

Finally, the parameters $p=163255597$, $\varepsilon=35261009$, $\eta=159772073$ supplied by the parameter deciding device 15
5 are supplied from the output device 18.

This time, the form of a second embodiment according to the present invention will be described in detail.

The form of the second embodiment according to
10 the present invention is a secure parameter generating method in an algebraic curve cryptography, comprising:
(a) a Stickelberger element computing procedure of requiring the prime numbers a and b respectively from the a -storing file 161 and the b -storing file 162 and
15 computing the Stickelberger element ω in the ab portion of the cyclotomic field;
(b) a procedure of storing the Stickelberger element ω computed in the above Stickelberger element computing procedure into the ω -storing file 163;
20 (c) a Jacobian addition candidate value computing procedure of requiring the prime number a , the prime number b , the size n of an encryption key, and the Stickelberger element ω respectively from the a -storing file 161, the b -storing file 162, the n -storing file 168,
25 and ω -storing file 163 and computing the Jacobian addition candidate value j as for the two different prime numbers a and b and the prime number p

corresponding to the Jacobian addition candidate value
j;

(d) a procedure of storing the prime number p and the
Jacobian addition candidate value j computed in the
5 above Jacobian addition candidate value computing
procedure, respectively into the p-storing file 167 and
the j-storing file 164;

(e) an order candidate value computing procedure of
requiring the prime number a, the prime number b, and
10 the Jacobian candidate value j respectively from the a-
storing file 161, the b-storing file 162, and the j-
storing file 164 and computing the class H consisting of
a plurality of candidate values for the order of the
Jacobian group of the algebraic curve specified by the
15 prime number a and the prime number b;

(f) a procedure of storing the class H computed in the
above order candidate value computing procedure into the
H-storing file 165;

(g) a security judging procedure of requiring the class
20 H from the H-storing file 165 and searching for the
candidate value h meeting the security condition such as
almost prime number characteristic;

(h) a procedure of storing the candidate value h found
in the above security judging procedure, into the h-
25 storing file 166; and

(i) a parameter deciding procedure of requiring the
prime number a, the prime number b, the prime number p,

and the candidate value h respectively from the a -
storing file 161, the b -storing file 162, the p -storing
file 167, and the h -storing file 166 and computing a
parameter of an algebraic curve whose order of the
5 Jacobian group is in accord with the candidate value h ,
of the algebraic curves specified by the prime number a ,
the prime number b , and the prime number p .

The form of a third embodiment according to the
present invention will be described in detail with
10 reference to the drawings, this time. Fig. 6 is a block
diagram showing the form of the third embodiment
according to the present invention.

With reference to Fig. 6, the form of the third
embodiment of the present invention is a storing medium
15 130 for storing a program for running the respective
procedures according to the form of the second
embodiment of the present invention, on a computer 100.
This program is executed after being loaded in a storage
of the computer 100.

20 The present invention is effective in enabling
the use of a higher and complicated algebraic curve
which couldn't be used, for an algebraic curve
cryptography, and improving the security of the
algebraic curve cryptography. This is because an
25 algebraic curve having a prime number substantially as
the order of the Jacobian group can be found efficiently
from the class of algebraic curves having the following

definition equation; $\alpha Y^a + \beta X^b + 1 = 0$, thereby expanding the range of the usable algebraic curves and dispersedly increasing the decoding work of a hacker.

Although the invention has been illustrated and described with respect to exemplary embodiment thereof, it should be understood by those skilled in the art that the foregoing and various other changes, omissions and additions may be made therein and thereto, without departing from the spirit and scope of the present invention. Therefore, the present invention should not be understood as limited to the specific embodiment set out above but to include all possible embodiments which can be embodied within a scope encompassed and equivalents thereof with respect to the feature set out in the appended claims.

WHAT IS CLAIMED IS:

1. A secure parameter generating device in an algebraic curve cryptography, comprising:

an input means for receiving two different prime numbers (a, b) specifying degree of complexity of a curve and size (n) of an encryption key to be used;

a Stickelberger element computing device for computing a Stickelberger element (ω) in an ab cyclotomic, based on the prime number (a) and the prime number (b);

a Jacobian addition candidate value computing device for computing Jacobian addition candidate value j corresponding to the two different prime numbers a and b, and a prime number p corresponding to the Jacobian addition candidate value j, based on the prime number (a), the prime number (b), the size (n) of an encryption key, and the Stickelberger element (ω);

an order candidate value computing device for computing a class H consisting of a plurality of candidate values for order of a Jacobian group of an algebraic curve specified by the prime number a and the prime number b, based on the prime number a, the prime number b, and the Jacobian addition candidate value j;

a security judging device for searching for a candidate value h meeting a security condition such as almost prime number characteristic from the class H,

according to the class H;

a parameter deciding device for computing a parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h,
30 of the algebraic curves specified by the prime number a, the prime number b, and the prime number p, based on the prime number a, the prime number b, the prime number p, and the candidate value h; and

an output device for supplying the parameter of
35 the algebraic curve computed by said parameter deciding device.

2. A secure parameter generating device in an algebraic curve cryptography as claimed in Claim 1, further comprising:

an a-storing means, a b-storing means, and an n-
5 storing means for respectively storing the prime number a, the prime number b, and the size n of the encryption key received by said input means;

a ω -storing means for storing a Stickelberger element ω computed by said Stickelberger element
10 computing device;

a p-storing means and a j-storing means for respectively storing the prime number p and the Jacobian addition candidate value j computed by said Jacobian addition candidate value computing device;

15 an H-storing means for storing the class H

computed by said order candidate value computing device;
and

an h-storing means for storing the candidate
value h found by said security judging device.

20

3. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,
further comprising:

said Stickelberger element computing device for
computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
(ζ is the primitive ab root of 1)), based on the prime
number a and the prime number b.

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4. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,
further comprising:

said Jacobian addition candidate value computing
device for generating α at random, which is an algebraic
integer γ generating a prime ideal of a cyclotomic K
generated by the primitive ab root of 1 and whose
absolute norm becomes the prime number p of bit length

5

2n/(a-1)(b-1) or so, based on the prime number a, the
10 prime number b, the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$.

5. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,
further comprising:

5 said Stickelberger element computing device for
computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
(ζ is the primitive ab root of 1)), based on the prime
number a and the prime number b; and

15 said Jacobian addition candidate value computing
device for generating α at random, which is an algebraic
integer γ generating a prime ideal of a cyclotomic K
generated by the primitive ab root of 1 and whose
absolute norm becomes the prime number p of bit length
2n/(a-1)(b-1) or so, based on the prime number a, the
20 prime number b, the size n of the encryption key,
and the Stickelberger element ω , and computing the

Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$.

6. A secure parameter generating device in an algebraic curve cryptography as claimed in Claim 1, further comprising:

said order candidate value computing device for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

7. A secure parameter generating device in an algebraic curve cryptography as claimed in Claim 1, further comprising:

said Stickelberger element computing device for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t

indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b ; and

15 said order candidate value computing device for
computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1
20 to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

8. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,
further comprising:

5 said Jacobian addition candidate value computing
device for generating α at random, which is an algebraic
integer γ generating a prime ideal of a cyclotomic K
generated by the primitive ab root of 1 and whose
absolute norm becomes the prime number p of bit length
 $2n/(a-1)(b-1)$ or so, based on the prime number a , the
10 prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$; and

said order candidate value computing device for
15 computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1
20 to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

9. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,
further comprising:

said Stickelberger element computing device for
5 computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
(ζ is the primitive ab root of 1)), based on the prime
number a and the prime number b ;

said Jacobian addition candidate value computing
15 device for generating α at random, which is an algebraic
integer γ generating a prime ideal of a cyclotomic K

generated by the primitive ab root of 1 and whose
absolute norm becomes the prime number p of bit length
 $2n/(a-1)(b-1)$ or so, based on the prime number a , the
20 prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$; and

said order candidate value computing device for
25 computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1
30 to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

10. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,
further comprising:

said parameter deciding device for requiring the
5 primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a , the prime number b , the prime number
 p , and the candidate value h , generating a random point
 G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$

10 $+ \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h -fold of an element in the Jacobian group
indicated by the point G , and supplying p , ζ_a^1 , and ζ_b^m
as the parameter of an algebraic curve whose order of
15 the Jacobian group is in accord with the candidate value
 h , of the algebraic curves specified by the prime number
 a and the prime number b if the result is equal to an
identity element in the Jacobian group.

11. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,
further comprising:

5 said Stickelberger element computing device for
computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
(ζ is the primitive ab root of 1)), based on the prime
number a and the prime number b ; and

15 said parameter deciding device for requiring the
primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a , the prime number b , the prime number

20 p, and the candidate value h, generating a random point
G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$
+ $\zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h-fold of an element in the Jacobian group
indicated by the point G, and supplying p, ζ_a^{-1} , and ζ_b^m
as the parameter of an algebraic curve whose order of
25 the Jacobian group is in accord with the candidate value
h, of the algebraic curves specified by the prime number
a and the prime number b if the result is equal to an
identity element in the Jacobian group.

12. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,
further comprising:

5 said Jacobian addition candidate value computing
device for generating α at random, which is an algebraic
integer γ generating a prime ideal of a cyclotomic K
generated by the primitive ab root of 1 and whose
absolute norm becomes the prime number p of bit length
 $2n/(a-1)(b-1)$ or so, based on the prime number a, the
10 prime number b, the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$; and

15 said parameter deciding device for requiring the
primitive a root ζ_a and the primitive b root ζ_b of 1

with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^l y^a + \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^l , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

13. A secure parameter generating device in an algebraic curve cryptography as claimed in Claim 1, further comprising:

said order candidate value computing device for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$; and

15 said parameter deciding device for requiring the
primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a, the prime number b, the prime number
p, and the candidate value h, generating a random point
G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$
20 + $\zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h-fold of an element in the Jacobian group
indicated by the point G, and supplying p, ζ_a^{-1} , and ζ_b^m
as the parameter of an algebraic curve whose order of
25 the Jacobian group is in accord with the candidate value
h, of the algebraic curves specified by the prime number
a and the prime number b if the result is equal to an
identity element in the Jacobian group.

14. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,
further comprising:

5 said Stickelberger element computing device for
computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic

(ζ is the primitive ab root of 1)), based on the prime number a and the prime number b ;

said Jacobian addition candidate value computing
15 device for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the
20 prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$; and

said parameter deciding device for requiring the
25 primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a + \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a
30 inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of
35 the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

15. A secure parameter generating device in an algebraic curve cryptography as claimed in Claim 1, further comprising:

said Stickelberger element computing device for
5 computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b ;

said order candidate value computing device for
15 computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1
20 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$; and

said parameter deciding device for requiring the
25 primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on

the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a + \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

16. A secure parameter generating device in an algebraic curve cryptography as claimed in Claim 1, further comprising:

said Jacobian addition candidate value computing device for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$;

said order candidate value computing device for

15 computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1
20 to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$; and

 said parameter deciding device for requiring the
25 primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a , the prime number b , the prime number
 p , and the candidate value h , generating a random point
 G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$
30 $+ \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h -fold of an element in the Jacobian group
indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m
as the parameter of an algebraic curve whose order of
35 the Jacobian group is in accord with the candidate value
 h , of the algebraic curves specified by the prime number
 a and the prime number b if the result is equal to an
identity element in the Jacobian group.

17. A secure parameter generating device in an
algebraic curve cryptography as claimed in Claim 1,

further comprising:

5 said Stickelberger element computing device for
computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
(ζ is the primitive ab root of 1)), based on the prime
number a and the prime number b ;

15 said Jacobian addition candidate value computing
device for generating α at random, which is an algebraic
integer γ generating a prime ideal of a cyclotomic K
generated by the primitive ab root of 1 and whose
absolute norm becomes the prime number p of bit length
 $2n/(a-1)(b-1)$ or so, based on the prime number a , the
20 prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$;

25 said order candidate value computing device for
computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1

30 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H=\{h_1, h_2, \dots, h_{2ab}\}$; and

35 said parameter deciding device for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$
40 $+ \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m as the parameter of an algebraic curve whose order of
45 the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

18. A secure parameter generating method in an algebraic curve, comprising the steps of:

5 a Stickelberger element computing procedure for computing a Stickelberger element ω in an ab cyclotomic, respectively based on two different prime numbers a and b specifying degree of complexity of curve;

a Jacobian addition candidate value computing

procedure for computing Jacobian addition candidate
value j corresponding to the two different prime numbers
10 a and b , and a prime number p corresponding to the
Jacobian addition candidate value j , respectively based
on the prime number a , the prime number b , the size n of
an encryption key, and the Stickelberger element ω ;

an order candidate value computing procedure for
15 computing a class H consisting of a plurality of
candidate values for order of a Jacobian group of an
algebraic curve specified by the prime number a and the
prime number b , respectively based on the prime number a ,
the prime number b , and the Jacobian addition candidate
20 value j ;

a security judging procedure for searching for a
candidate value h meeting a security condition such as
almost prime number characteristic from the class H ,
according to the class H ; and

25 a parameter deciding procedure for computing a
parameter of an algebraic curve whose order of the
Jacobian group is in accord with the candidate value h ,
of the algebraic curves specified by the prime number a ,
the prime number b , and the prime number p , respectively
30 based on the prime number a , the prime number b , the
prime number p , and the candidate value h .

19. A secure parameter generating method in an
algebraic curve cryptography as claimed in Claim 18,

further comprising:

5 a procedure for storing a Stickelberger element ω computed by said Stickelberger element computing procedure into said ω -storing means;

10 a procedure for respectively storing the prime number p and the Jacobian addition candidate value j computed by said Jacobian addition candidate value computing procedure into said p -storing means and j -storing means;

a procedure for storing the class H computed by said order candidate value computing procedure into said H -storing means; and

15 a procedure for storing the candidate value h found by said security judging procedure into said h -storing means.

20. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

5 said Stickelberger element computing procedure for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic

(ζ is the primitive ab root of 1)), based on the prime number a and the prime number b .

21. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

said Jacobian addition candidate value computing procedure for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$.

22. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

said Stickelberger element computing procedure for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t

indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b; and

said Jacobian addition candidate value computing
15 procedure for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a,
20 the prime number b, the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$.

23. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

said order candidate value computing procedure
5 for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b, using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1
10 to 2ab inclusively, when ζ is the primitive ab root of 1, based on the prime number a, the prime number b, and the Jacobian addition candidate value j, and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

24. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

said Stickelberger element computing procedure
5 for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b ; and

said order candidate value computing procedure
15 for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1
20 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

25. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18,

further comprising:

5 said Jacobian addition candidate value computing
procedure for generating α at random, which is an
algebraic integer γ generating a prime ideal of a
cyclotomic K generated by the primitive ab root of 1 and
whose absolute norm becomes the prime number p of bit
length $2n/(a-1)(b-1)$ or so, based on the prime number a ,
10 the prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$; and

15 said order candidate value computing procedure
for computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-$
 $\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1
20 to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$.

26. A secure parameter generating method in an
algebraic curve cryptography as claimed in Claim 18,
further comprising:

5 said Stickelberger element computing procedure
for computing the Stickelberger element ω by use of the

equation $\omega = \sum t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t-1}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b ;

said Jacobian addition candidate value computing procedure for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$; and

said order candidate value computing procedure for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the

class of the candidate values, $H=\{h_1, h_2, \dots, h_{2ab}\}$.

27. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

said parameter deciding procedure for requiring
5 the primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a, the prime number b, the prime number
p, and the candidate value h, generating a random point
G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$
10 + $\zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h-fold of an element in the Jacobian group
indicated by the point G, and supplying p, ζ_a^{-1} , and ζ_b^m
as the parameter of an algebraic curve whose order of
15 the Jacobian group is in accord with the candidate value
h, of the algebraic curves specified by the prime number
a and the prime number b if the result is equal to an
identity element in the Jacobian group.

28. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

said Stickelberger element computing procedure
5 for computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs

on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b ; and

said parameter deciding procedure for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a + \zeta_b^{-m} X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^{-m} as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

29. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

said Jacobian addition candidate value computing

5 procedure for generating α at random, which is an
algebraic integer γ generating a prime ideal of a
cyclotomic K generated by the primitive ab root of 1 and
whose absolute norm becomes the prime number p of bit
length $2n/(a-1)(b-1)$ or so, based on the prime number a ,
10 the prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$; and

15 said parameter deciding procedure for requiring
the primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a , the prime number b , the prime number
 p , and the candidate value h , generating a random point
 G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$
20 $+ \zeta_b^m X_b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h -fold of an element in the Jacobian group
indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m
as the parameter of an algebraic curve whose order of
25 the Jacobian group is in accord with the candidate value
 h , of the algebraic curves specified by the prime number
 a and the prime number b if the result is equal to an
identity element in the Jacobian group.

30. A secure parameter generating method in an
algebraic curve cryptography as claimed in Claim 18,

further comprising:

5 said order candidate value computing procedure
for computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1
10 to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$; and
15 said parameter deciding procedure for requiring
the primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a , the prime number b , the prime number
 p , and the candidate value h , generating a random point
 G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$
20 + $\zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h -fold of an element in the Jacobian group
indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m
as the parameter of an algebraic curve whose order of
25 the Jacobian group is in accord with the candidate value
 h , of the algebraic curves specified by the prime number
 a and the prime number b if the result is equal to an
identity element in the Jacobian group.

31. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

said Stickelberger element computing procedure
5 for computing the Stickelberger element ω by use of the equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs on a typical series of irreducible residue class with ab used as a divisor, $[\lambda]$ indicates the maximum integer not exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic (ζ is the primitive ab root of 1)), based on the prime number a and the prime number b ;

said Jacobian addition candidate value computing
15 procedure for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit length $2n/(a-1)(b-1)$ or so, based on the prime number a ,
20 the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$; and

said parameter deciding procedure for requiring
25 the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number

30 p, and the candidate value h, generating a random point
G over an algebraic curve defined by the equation $\zeta_a^{-1} y^a$
+ $\zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h-fold of an element in the Jacobian group
indicated by the point G, and supplying p, ζ_a^{-1} , and ζ_b^m
as the parameter of an algebraic curve whose order of
35 the Jacobian group is in accord with the candidate value
h, of the algebraic curves specified by the prime number
a and the prime number b if the result is equal to an
identity element in the Jacobian group.

32. A secure parameter generating method in an
algebraic curve cryptography as claimed in Claim 18,
further comprising:

5 said Stickelberger element computing procedure
for computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
(ζ is the primitive ab root of 1)), based on the prime
number a and the prime number b;

15 said order candidate value computing procedure
for computing a candidate value h_k for the order of the

Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$; and

said parameter deciding procedure for requiring the primitive a root ζ_a and the primitive b root ζ_b of 1 with the prime number p used as the divisor, based on the prime number a , the prime number b , the prime number p , and the candidate value h , generating a random point G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a + \zeta_b^{-m} X^b + 1 = 0$, as for each integer l from 1 to a inclusively and each integer m from 1 to b inclusively, computing the h -fold of an element in the Jacobian group indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^{-m} as the parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

33. A secure parameter generating method in an algebraic curve cryptography as claimed in Claim 18, further comprising:

said Jacobian addition candidate value computing
5 procedure for generating α at random, which is an
algebraic integer γ generating a prime ideal of a
cyclotomic K generated by the primitive ab root of 1 and
whose absolute norm becomes the prime number p of bit
length $2n/(a-1)(b-1)$ or so, based on the prime number a ,
10 the prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$;

said order candidate value computing procedure
15 for computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{\{K|Q\}}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1
20 to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$; and

said parameter deciding procedure for requiring
25 the primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a , the prime number b , the prime number
 p , and the candidate value h , generating a random point
 G over an algebraic curve defined by the equation $\zeta_a^{-1} y^a$
30 $+ \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a

inclusively and each integer m from 1 to b inclusively,
computing the h -fold of an element in the Jacobian group
indicated by the point G , and supplying p , ζ_a^1 , and ζ_b^m
as the parameter of an algebraic curve whose order of
the Jacobian group is in accord with the candidate value
35 h , of the algebraic curves specified by the prime number
 a and the prime number b if the result is equal to an
identity element in the Jacobian group.

34. A secure parameter generating method in an
algebraic curve cryptography as claimed in Claim 18,
further comprising:

said Stickelberger element computing procedure
5 for computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
10 fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
(ζ is the primitive ab root of 1)), based on the prime
number a and the prime number b ;

said Jacobian addition candidate value computing
15 procedure for generating α at random, which is an
algebraic integer γ generating a prime ideal of a
cyclotomic K generated by the primitive ab root of 1 and
whose absolute norm becomes the prime number p of bit

length $2n/(a-1)(b-1)$ or so, based on the prime number a ,
20 the prime number b , the size n of the encryption key,
and the Stickelberger element ω , and computing the
Jacobian addition candidate value j by use of the
equation $j = \gamma^\omega$;

said order candidate value computing procedure
25 for computing a candidate value h_k for the order of the
Jacobian group of an algebraic curve specified by the
parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{K|Q}$ is a norm mapping in the ab
cyclotomic K), as for each k that is an integer from 1
30 to $2ab$ inclusively, when ζ is the primitive ab root of 1,
based on the prime number a , the prime number b , and the
Jacobian addition candidate value j , and computing the
class of the candidate values, $H = \{h_1, h_2, \dots, h_{2ab}\}$; and

said parameter deciding procedure for requiring
35 the primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a , the prime number b , the prime number
 p , and the candidate value h , generating a random point
 G over an algebraic curve defined by the equation $\zeta_a^{-1} Y^a$
40 $+ \zeta_b^m X^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h -fold of an element in the Jacobian group
indicated by the point G , and supplying p , ζ_a^{-1} , and ζ_b^m
as the parameter of an algebraic curve whose order of
45 the Jacobian group is in accord with the candidate value

h, of the algebraic curves specified by the prime number a and the prime number b if the result is equal to an identity element in the Jacobian group.

35. A computer readable memory storing a program for generating a secure parameter in an algebraic curve cryptography, to run the program on a computer,

the program comprising the steps of:

5 a Stickelberger element computing procedure for computing a Stickelberger element ω in an ab cyclotomic, respectively based on two different prime numbers a and b specifying degree of complexity of curve;

10 a Jacobian addition candidate value computing procedure for computing Jacobian addition candidate value j corresponding to the two different prime numbers a and b, and a prime number p corresponding to the Jacobian addition candidate value j, respectively based on the prime number a, the prime number b, the size n of an encryption key, and the Stickelberger element ω ;

15 an order candidate value computing procedure for computing a class H consisting of a plurality of candidate values for order of a Jacobian group of an algebraic curve specified by the prime number a and the prime number b, respectively based on the prime number a, the prime number b, and the Jacobian addition candidate value j;

20 a security judging procedure for searching for a

candidate value h meeting a security condition such as
25 almost prime number characteristic from the class H ,
according to the class H ; and

a parameter deciding procedure for computing a
parameter of an algebraic curve whose order of the
Jacobian group is in accord with the candidate value h ,
30 of the algebraic curves specified by the prime number a ,
the prime number b , and the prime number p , respectively
based on the prime number a , the prime number b , the
prime number p , and the candidate value h .

~~36.~~ A computer readable memory storing a program for
generating a secure parameter in an algebraic curve
cryptography,

the program comprising the steps of:

5 said Stickelberger element computing procedure
for computing the Stickelberger element ω by use of the
equation $\omega = \sum_t [\langle t/a \rangle + \langle t/b \rangle] \sigma_{-t^{-1}}$ (where, t runs
on a typical series of irreducible residue class with ab
used as a divisor, $[\lambda]$ indicates the maximum integer not
10 exceeding a rational number λ , $\langle \lambda \rangle$ indicates a
fractional portion $\lambda - [\lambda]$ of the rational number λ , σ_t
indicates Galois mapping $\zeta \rightarrow \zeta^t$ in the ab cyclotomic
(ζ is the primitive ab root of 1)), based on the prime
number a and the prime number b .

15

~~37.~~ A computer readable memory storing a program for

generating a secure parameter in an algebraic curve cryptography,

the program comprising the steps of:

5 said Jacobian addition candidate value computing procedure for generating α at random, which is an algebraic integer γ generating a prime ideal of a cyclotomic K generated by the primitive ab root of 1 and whose absolute norm becomes the prime number p of bit
10 length $2n/(a-1)(b-1)$ or so, based on the prime number a , the prime number b , the size n of the encryption key, and the Stickelberger element ω , and computing the Jacobian addition candidate value j by use of the equation $j = \gamma^\omega$.

15 38. A computer readable memory storing a program for generating a secure parameter in an algebraic curve cryptography,

the program comprising the steps of:

5 said order candidate value computing procedure for computing a candidate value h_k for the order of the Jacobian group of an algebraic curve specified by the parameters a and b , using the equation $h_k = \text{Norm}_{K|Q}(1 + (-\zeta)^k j)$ (where $\text{Norm}_{\{K|Q\}}$ is a norm mapping in the ab
10 cyclotomic K), as for each k that is an integer from 1 to $2ab$ inclusively, when ζ is the primitive ab root of 1, based on the prime number a , the prime number b , and the Jacobian addition candidate value j , and computing the

class of the candidate values, $H=\{h_1, h_2, \dots, h_{2ab}\}$.

15

39. A computer readable memory storing a program for
generating a secure parameter in an algebraic curve
cryptography,

the program comprising the steps of:

5

said parameter deciding procedure for requiring
the primitive a root ζ_a and the primitive b root ζ_b of 1
with the prime number p used as the divisor, based on
the prime number a, the prime number b, the prime number
p, and the candidate value h, generating a random point
10 G over an algebraic curve defined by the equation $\zeta_a^{-1} y^a$
 $+ \zeta_b^m x^b + 1 = 0$, as for each integer l from 1 to a
inclusively and each integer m from 1 to b inclusively,
computing the h-fold of an element in the Jacobian group
indicated by the point G, and supplying p, ζ_a^{-1} , and ζ_b^m
15 as the parameter of an algebraic curve whose order of
the Jacobian group is in accord with the candidate value
h, of the algebraic curves specified by the prime number
a and the prime number b if the result is equal to an
identity element in the Jacobian group.

ABSTRACT OF THE DISCLOSURE

The Stickelberger element computing device computes a Stickelberger element ω in an ab cyclotomic; the Jacobian addition candidate value computing device computes the Jacobian addition candidate value j and a prime number p corresponding to the Jacobian addition candidate value j , based on the prime number a , the prime number b , the size n of an encryption key, and the Stickelberger element ω ; the order candidate value computing device computes a class H consisting of a plurality of candidate values for the order of the Jacobian group of an algebraic curve, based on the prime number a , the prime number b , and the Jacobian addition candidate value j ; the security judging device searches for a candidate value h meeting a security condition such as almost prime number characteristic from the class H ; and the parameter deciding device computes a parameter of an algebraic curve whose order of the Jacobian group is in accord with the candidate value h , of the algebraic curves specified by the prime number a , the prime number b , and the prime number p .

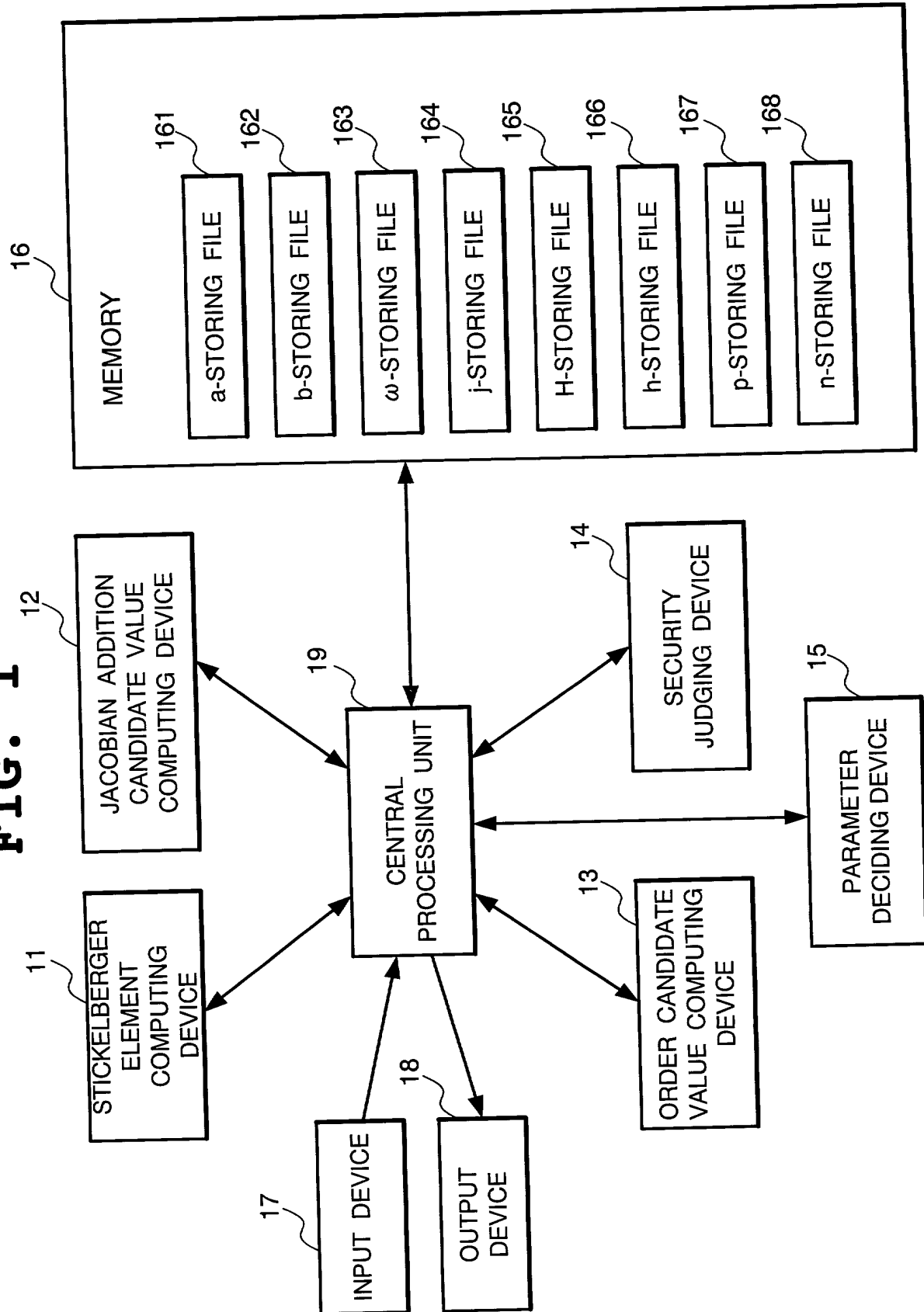
FIG. 1

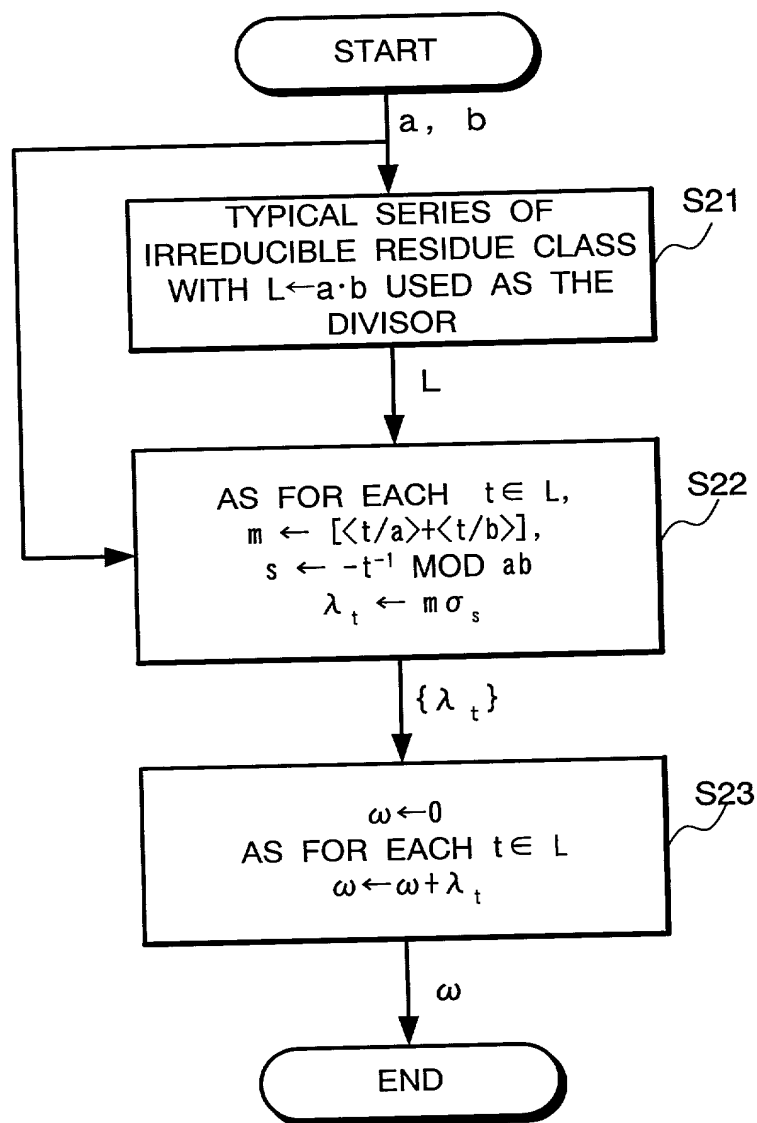
FIG. 2

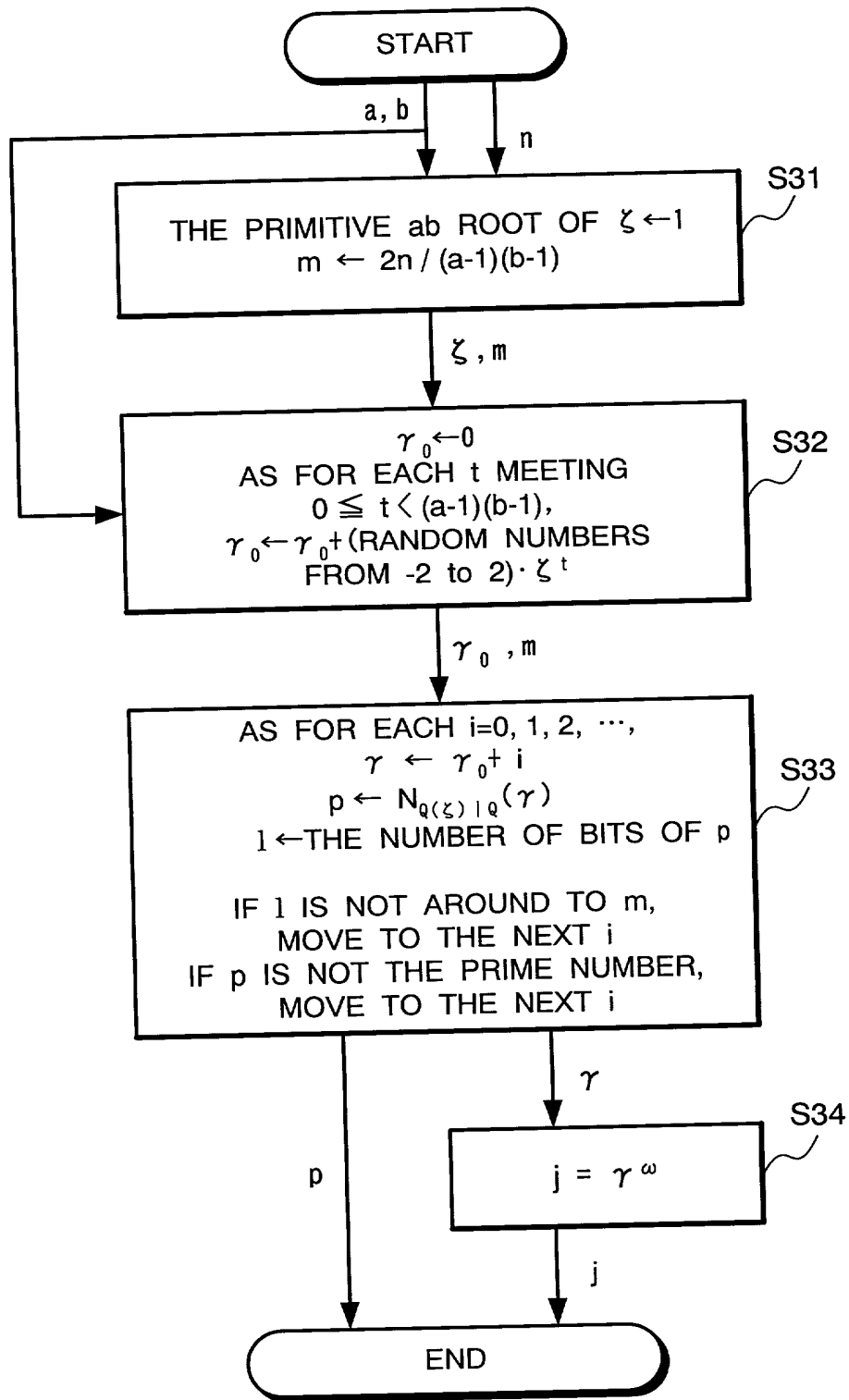
FIG. 3

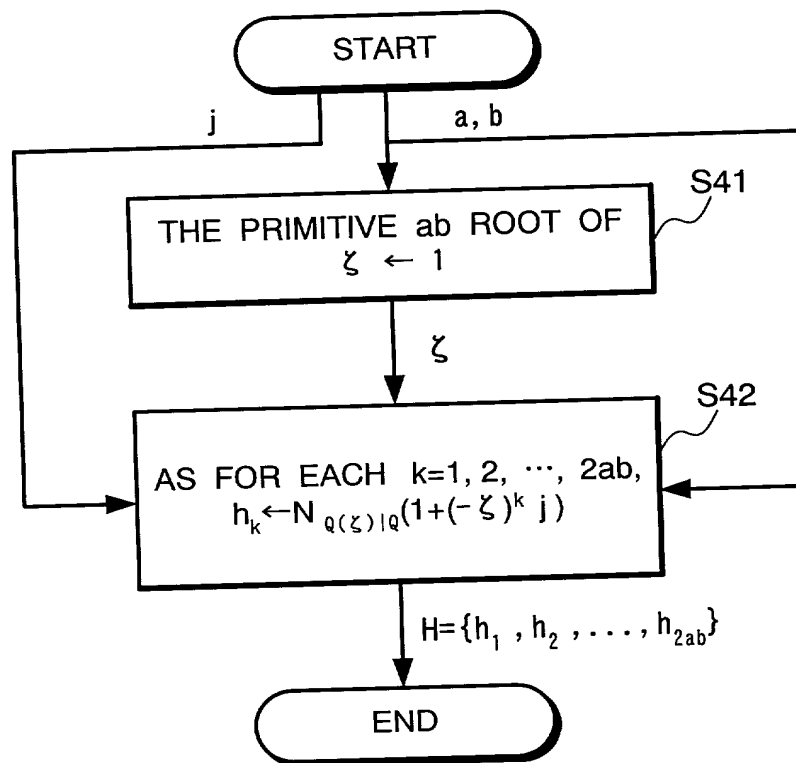
FIG. 4

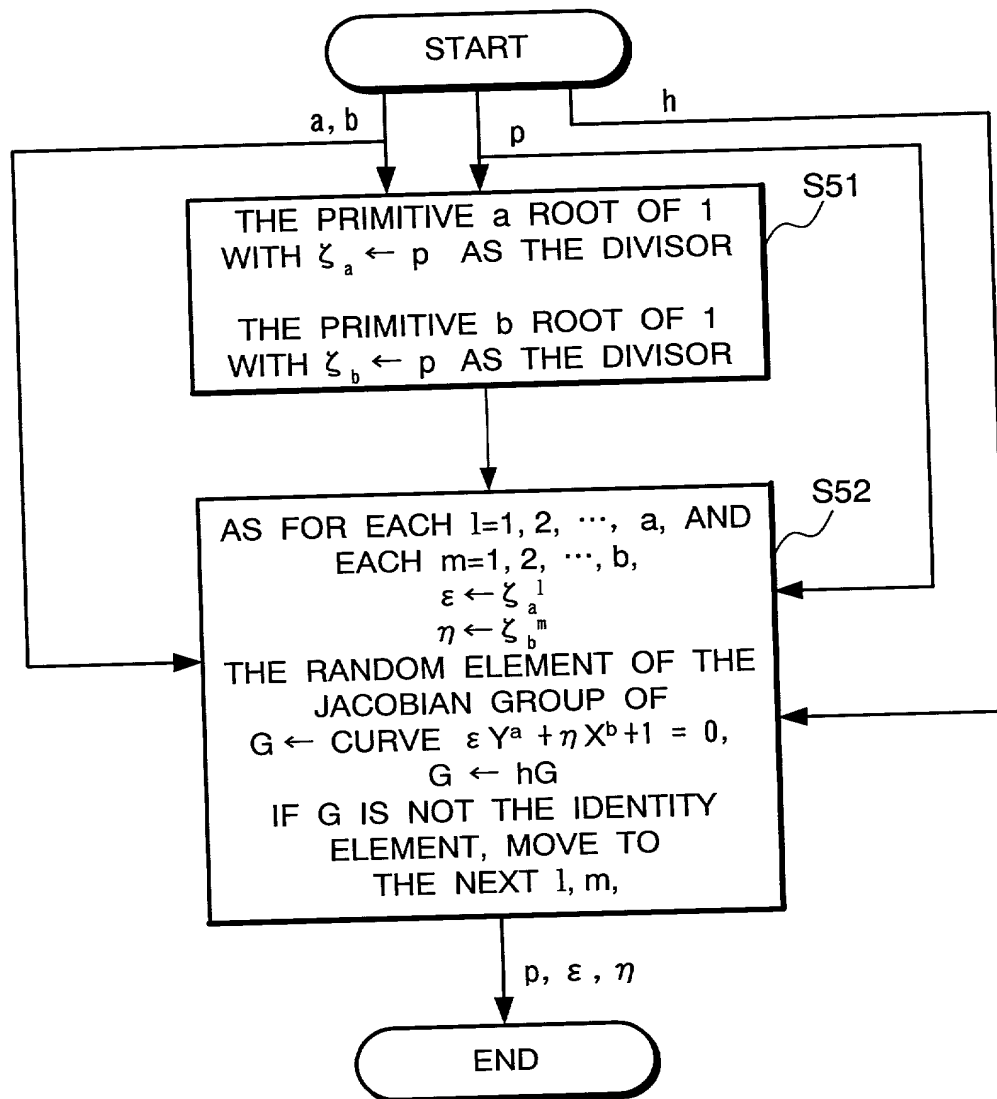
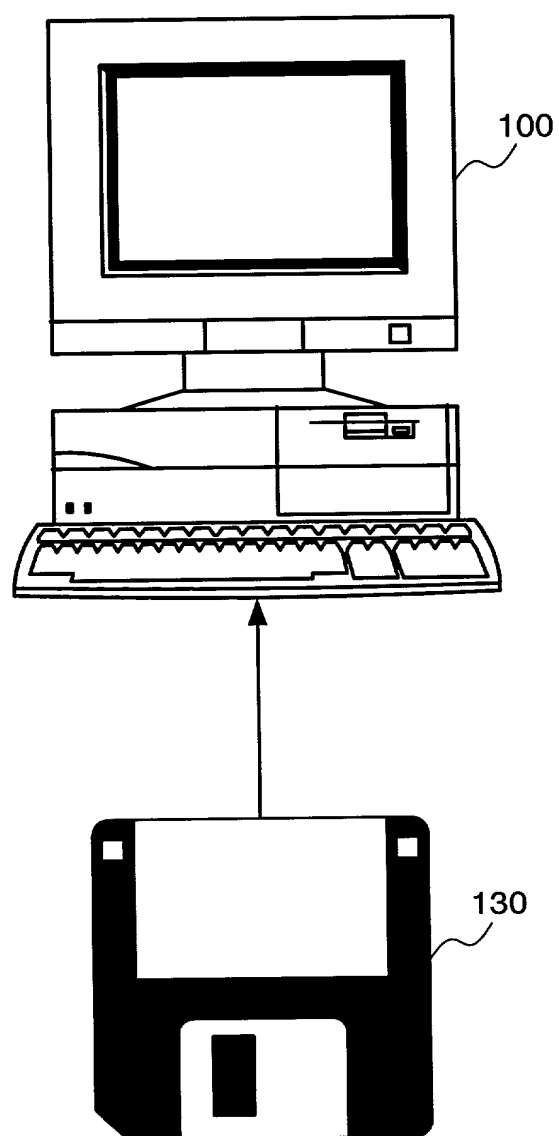
FIG. 5

FIG. 6

DECLARATION AND POWER OF ATTORNEY

As a below named inventor, I hereby declare that:

My residence, post office address and citizenship are as stated below next to my name.

I believe I am the original, first and sole inventor (if only one name is listed below) or an original, first and joint inventor (if plural names are listed below) of the subject matter which is claimed and for which a patent is sought on the invention entitled:

SECURE PARAMETER GENERATING DEVICE AND PARAMETER GENERATING METHOD IN

the specification of which is attached hereto unless the following box is checked:

ALGEBRAIC CURVE CRYPTOGRAPHY

☐ was filed on _____ as United States Application Number or PCT International Application Number _____ and was amended on _____ (if applicable).

I hereby state that I have reviewed and understand the contents of the above-identified specification, including the claims, as amended by any amendment referred to above.

I acknowledge the duty to disclose information which is known by me to be material to patentability as defined in Title 37, Code of Federal Regulations § 1.56.

I hereby claim foreign priority benefits under Title 35, United States Code, § 119(a)-(d) or § 365(b) of any foreign application(s) for patent or inventor's certificate, or § 365(a) of any PCT International application which designated at least one country other than the United States, listed below and have also identified below any foreign application for patent or inventor's certificate, or PCT International application having a filing date before that of the application on which priority is claimed:

PRIOR FOREIGN APPLICATION(S)

NUMBER	COUNTRY	DAY/MONTH/YEAR FILED	PRIORITY CLAIMED
11-242075	Japan	27/August/1999	Yes

I hereby claim the benefit under Title 35, United States Code § 119(e) of any United States provisional application(s) listed below.

APPLICATION NO.	FILING DATE

I hereby claim the benefit under Title 35, United States Code, § 120 of any United States application(s), or § 365(c) of any PCT International application designating the United States, listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States or PCT International application in the manner provided by the first paragraph of Title 35, United States Code, § 112, I acknowledge the duty to disclose information which is known by me to be material to patentability as defined in Title 37, Code of Federal Regulations § 1.56 which became available between the filing date of the prior application and the national or PCT International filing date of this application:

APPLICATION SERIAL NO.	FILING DATE	STATUS: PATENTED, PENDING, ABANDONED

I hereby appoint as my attorneys, with full powers of substitution and revocation, to prosecute this application and transact all business in the Patent and Trademark Office connected therewith: Stephen A. Bent, Reg. No. 29,768; David A. Blumenthal, Reg. No. 26,257; John J. Feldhaus, Reg. No. 28,822; Donald D. Jeffery, Reg. No. 19,980; Eugene M. Lee, Reg. No. 32,039; Peter G. Mack, Reg. No. 26,001; Brian J. McNamara, Reg. No. 32,789; Sybil Meloy, Reg. No. 22,749; George E. Quillin, Reg. No. 32,792; Colin G. Sandercock, Reg. No. 31,298; Bernhard D. Saxe, Reg. No. 28,665; Charles F. Schill, Reg. No. 27,590; Richard L. Schwaab, Reg. No. 25,479; Arthur Schwartz, Reg. No. 22,115; Harold C. Wegner, Reg. No. 25,258.

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I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

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Residence Address	Country of Citizenship	
Post Office Address		

Full Name of Fourth Inventor	Signature of Fourth Inventor	Date
Residence Address	Country of Citizenship	
Post Office Address		

Full Name of Fifth Inventor	Signature of Fifth Inventor	Date
Residence Address	Country of Citizenship	
Post Office Address		